

Purpose:

Examine Elastic Constants

Verify wave equation for several cases

Review Complex Number Mathematics

- Q. 1 (a) Find or derive the relationship between Poisson's ratio and  $V_p$ , and  $V_s$   
 (If you do not derive this relationship, reference your source and verify that it holds true.)
- (b) Plot Poisson's ratio versus  $V_p/V_s$  ratio for  $V_p/V_s$  ratios extending from -5 to +5  
 (c) Indicate the location of an ideal Poisson solid and a liquid.  
 (d) Explain the existence of the asymptotes.  
 (e) What is Poisson's ratio for shale in the Gulf of Mexico

(use Matlab, Excel or Mathematica and cite your sources)

Q 2. Substitute the following equations back into the wave equation to show that they are indeed valid solutions to the wave equation:

$$V_p = \sqrt{\frac{k + \frac{4}{3}\mu}{\rho}}, \quad V_s = \sqrt{\frac{\mu}{\rho}}$$

Hint: Substitute these equations into the following versions of the elastic wave equation, which we have already seen:

$$\begin{aligned} \rho \frac{\partial^2 \bar{\Omega}}{\partial t^2} &= -\mu \nabla \times (\nabla \times \bar{\Omega}) \\ &= -\mu \left\{ \nabla (\nabla \cdot [(\nabla \times \bar{\Omega})]) \right\} + \nabla^2 \bar{\Omega} \\ &= -\frac{\mu}{\rho} \bar{\Omega} \end{aligned} \quad (\text{for } V_{\text{shear}})$$

$$\frac{\rho}{\lambda + 2\mu} \ddot{\Theta} = \nabla^2 \Theta$$

(for V acoustic)

Q. 3 Show the following is true algebraically and graphically using an Argand diagram

$$\frac{e^{i\theta} + e^{-i\theta}}{2} = \cos \theta$$

$$\frac{e^{i\theta} - e^{-i\theta}}{2} = \sin \theta$$